

## Comparison of the Vibration Frequencies of [6] Cyclacene (Zigzag, Armchair and Chiral) Monoring Molecules

Rehab M. Kubba

*College of Science, University of Baghdad*

Huda N. AL-Ani

Muthana Shanshal

*Author to whom correspondence to be mailed.*

(NJC)

(Receved on 13/1/2011 )

(Accepted for publication 27/9 /2011)

### Abstract

The (3N-6) vibration frequencies and IR-absorption intensities of [6] Cyclacene (zigzag, armchair and chiral) monoring molecules were calculated applying Density Functional Theory (DFT) of the type (B3LYP) and a Gaussian basis (6-311G) method. Comparison of the results showed that, similar to the polyaromatic hydrocarbons, the following relations hold:

$v_{\text{sym. CH str.}} > v_{\text{asym. CH str.}}$

and,

$v_{\text{sym. CC str.}} > v_{\text{asym. CC str.}}$  i. e.,

$v_{\text{sym. CC str. (axial)}} > v_{\text{asym. CC str. (axial)}} > v_{\text{asym. CC str. (circumferential)}}$  in the zigzag molecule, where axial are the vertical C-C<sub>a</sub> bonds (annular bonds) in the rings and circumferential C-C<sub>c</sub> are the outer ring bonds. The relation for the C-C str. is reversed in the armchair and the chiral molecules, since the C-C<sub>a</sub> bonds are converted to C-C<sub>c</sub> bonds in the armchair and chiral cyclacenes. The results include the assignment of all puckering, breathing and clock-anticlockwise bending vibrations. They allow a comparative view of the charge density at the carbon atoms too.

الخلاصة

(3N-6) (Armchair Chiral Zig-Zag 6 - )

.DFT (B3LYP/6-311G)

(C-C)

(C-H)

( $\delta$ CC) ( $\delta$ CH)

:

$v_{\text{sym. CH str.}} > v_{\text{asym. CH str.}}$

$v_{\text{sym}} \cdot \text{CC str.} > v_{\text{asym}} \cdot \text{CC str.}$  i. e.,  
 $v_{\text{sym}} \cdot \text{CC str. (axial.)} > v_{\text{asym}} \cdot \text{CC str. (axial)} > v_{\text{asym}} \cdot \text{CC str. (circumferential)}$

C-C<sub>c</sub>                      zig zag                      C-C<sub>a</sub>  
 Armchair    Chiral

## Introduction

Single wall carbon nanotubes (SWCNTs) are formed from folded sheets of annulated six membered aromatic rings<sup>[1]</sup>. The hybridization of each carbon atom in the sheet is sp<sup>2</sup><sup>[2]</sup>. They are of aromatic character, similar to graphite, and possess conjugated C-C bonds<sup>[3]</sup>. Their aromaticity is determined by the space distribution of the atoms, the nature of their molecular orbitals, their symmetry and chirality<sup>[4]</sup>. Various studies appeared in former years for the physical properties of the nanotubes<sup>[5-10]</sup>.

Cyclacenes are monoring segments of carbon nanotubes (CNT), Fig.1. Generally, attempts to synthesize them failed, with the exceptions of few cases<sup>[11]</sup>. An approach for their chemical stabilization was suggested<sup>[12]</sup>. It should facilitate their synthesis. For the cyclacene molecules with different ring size, numerous theoretical studies had been published<sup>[11]</sup>. However, no thorough treatment, including symmetry assignments for their

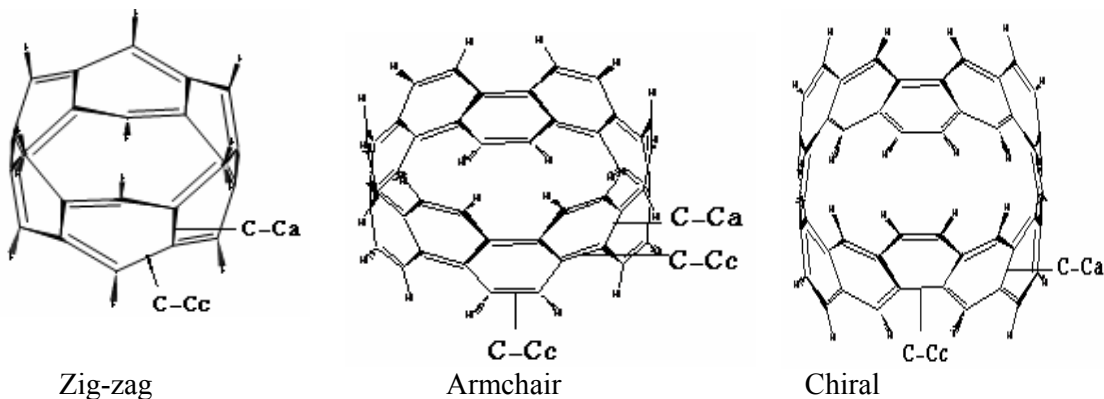
vibration frequencies appeared. Comparison of their vibration frequency values with those of the nanotubes and the planar polyaromatic hydrocarbons should help to estimate the strength of their total force field strength. For this purpose a complete normal coordinate analysis is required. In this work the quantum mechanical Density Functional Theory (DFT) method<sup>[13]</sup>, is applied, in the form of the B3LYP approach<sup>[14]</sup> and the 6-311G Gaussian bases<sup>[15]</sup> is utilized.

## Methods of calculation.

G03 program of Pople et al.<sup>[17]</sup> was applied throughout the present work.

## Results and Discussion.

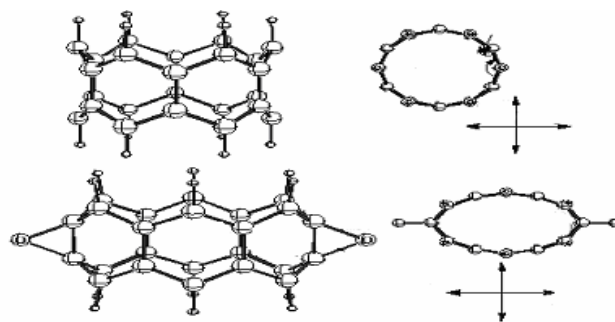
To study the vibration motions of such molecules, one has to define its geometric parameters, and has to distinguish between the axial CC (C-Caxial) and circumferential CC (C-C<sub>c</sub>) bonds. Figure 1 shows the two types of bonds in the different cyclacene rings.



**Figure 1: Structure of [6] Cyclacene (zigzag, armchair and chiral) monoring molecules, indicating the two types of C-C bonds; C-Caxial (C-C<sub>a</sub>) and C-circumferential (C-C<sub>c</sub>).**

Obviously, the vibration of a nanotube as well as cyclacenes, causes a deformation in its geometry Fig. 2.

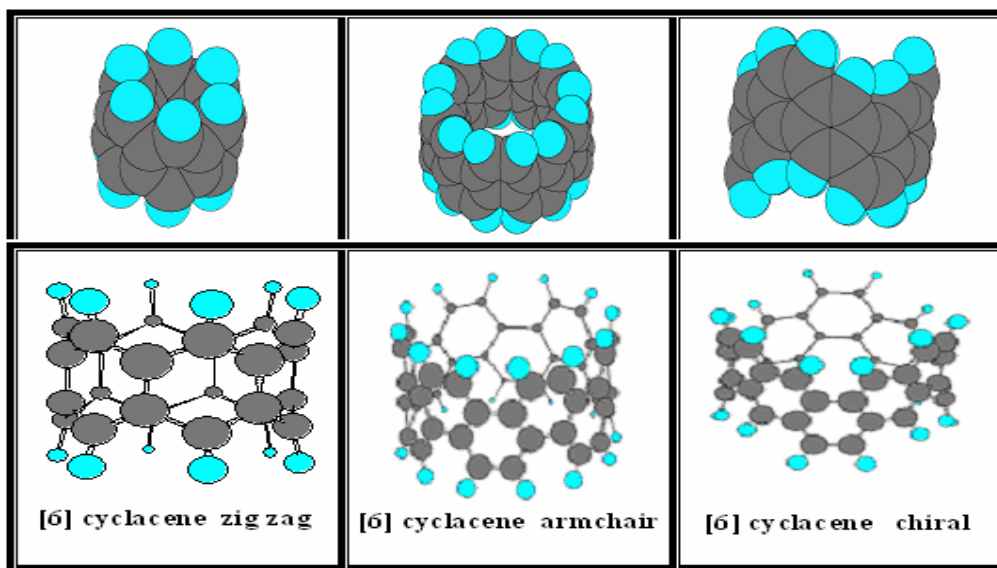
Structure deformation is expected to change their thermal and electronic properties<sup>[18]</sup> too.



**Figure 2: Structure deformation of a [6] Cyclacene (zigzag) monoring molecule as caused by its vibration motion.**

Basic vibrations of CNTs were measured and assigned as breathing, puckering and clock-anti-clockwise deformation modes<sup>[19]</sup>. The frequencies of their IR active vibrations range between (873-1557 cm<sup>-1</sup>)<sup>[20]</sup>. They are considered as finger print vibrations for the carbon nanotubes (CNTs)<sup>[21]</sup>. Measurements

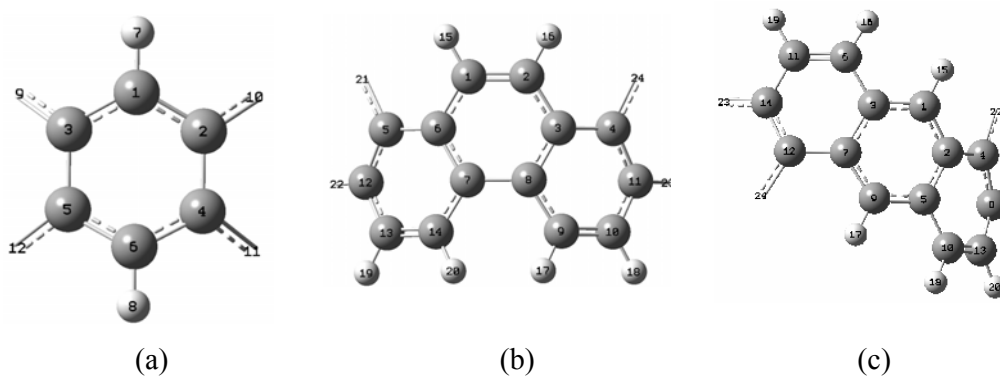
were done at 6°K to study the impact of the puckering distortion on the electronic properties of CNTs<sup>[22-23]</sup>. [6] cyclacene (zigzag, armchair, chiral) molecules are composed of annulated six membered aromatic rings. Their (DFT) calculated equilibrium geometry shows D<sub>6h</sub>, D<sub>6d</sub>, D<sub>3d</sub> symmetry respectively<sup>[24]</sup>, Figure 3.



**Figure 3: Equilibrium geometry for [6] Cyclacene (zigzag, armchair and chiral) monoring molecules.**

Due to their symmetries  $D_{6h}$ ,  $D_{6d}$  and  $D_{3d}$ , figure 4 shows repetitive sections of [6] Cyclacene monoring molecules,

and Table 1 shows some of their calculated geometric parameters.



**Figure 4: Repetitive sections of the bonds and angles of [6] Cyclacene ((a) zigzag, (b) armchair and (c) chiral) monoring molecules.**

**Table 1: DFT calculated bond distances of [6] Cyclacene (zigzag, armchair and chiral) monoring molecules. .**

Molecule	Diameter (Å)	Length (Å <sup>0</sup> )	C---Ca (Å)	C---Ca (Å)	C---Cc (Å)	C=Cc (Å)	C-Cc (Å)	C-H (Å)
[6] Cyclacene zig-zag (D <sub>6h</sub> )	5.183	4.972	1.446	-----	1.413	-----	-----	1.094
[6] Cyclacene armchair (D <sub>6d</sub> )	8.760	5.532	1.435	1.417	-----	1.366	1.452	1.080
[6] Cyclacene chiral (D <sub>3d</sub> )	8.758	6.758	C--C 1.433 C-C 1.449	1.403	1.454	1.356	1.471	=CH 1.082 --CH 1.081

As shown in (Table-1) the C-Ca bonds in the zigzag molecule are single bonds. They are longer than the C-Cc bonds connected to them. The C-Ca bonds in the armchair molecule are essential single bonds, and the C-Cc bonds are either double or single bonds. For the chiral molecule the C-Ca bonds are either single or conjugated and C-Cc bonds are of the three types; double, single and conjugated.

#### Vibration frequencies of [6] Cyclacene (zigzag, armchair and chiral).

##### -For zig-zag molecule:

The [6] Cyclacene (zigzag) molecule posses 102 fundamental vibrations. Inspection of its irreducible representations, as defined by the symmetry character table, results in the following modes of vibration;

$$\Gamma_{\text{vibration}} = \Gamma_{\text{total}} - (\Gamma_{\text{rotation}} + \Gamma_{\text{translation}}) = 3N - 6 = 108 - 6 = 102 = 6A_{1g} + 2A_{2g} + 4B_{1u} + 5B_{2u} + 8E_{1u} +$$

$$9E_{2g} + 3A_{1u} + 5A_{2u} + 5B_{1g} + 4B_{2g} + 8E_{1g} + 9E_{2u}$$

Relative to the  $\sigma_h$  reflection the vibration modes are classified as symmetric and antisymmetric modes;

**a- symmetric modes with respect to  $\sigma_h$  (+ $\sigma_h$ ).**

$$\Gamma_{+\sigma_h} = 6A_{1g} + 2A_{2g} + 5B_{1u} + 4B_{2u} + 8E_{1u} + 9E_{2g} \text{ ( In-plane } \sigma_h \text{ modes of vibrations)}$$

**b- antisymmetric modes with respect to  $\sigma_h$  (- $\sigma_h$ ).**

$$\Gamma_{-\sigma_h} = 3A_{1u} + 5A_{2u} + 4B_{1g} + 5B_{2g} + 8E_{1g} + 9E_{2u} \text{ (Out of plane } \sigma_h \text{ modes of vibrations)}$$

These are 51 modes of vibration in number, of which 24 are Raman active (6A<sub>1g</sub> (polarized) + 9E<sub>2g</sub> (depolarized)), and 18 IR active (9E<sub>1u</sub>).

**-For armchair molecule:**

$$\Gamma_{\text{vibration}} = 210 = 9A_1 + 8A_2 + 9B_1 + 8B_2 + 17E_1 + 18E_2 + 18E_3 + 18E_4 + 17E_5$$

These are 79 Raman active ( $9A_1$  (polarized) +  $17E_5$ ,  $18E_1$  (depolarized)), and 44 IR active ( $8B_2$ ,  $18E_{1u}$ ).

**-For chiral molecule:**

$$\Gamma_{\text{vib}} = 210 = 18A_{1g} + 35E_g + 17A_{2u} + 35E_u + 17A_{2g} + 18A_{1u}$$

These are 88 Raman active ( $18A_{1g}$  (polarized) +  $35E_g$  (depolarized)), 87 IR active ( $17A_{2u}$  +  $35E_u$ ) and 35 Raman and IR inactive ( $17A_{2g}$ ,

$18A_{1u}$ ). Their assignments are as follows:

**CH stretching vibrations****-For the zigzag molecule:**

Their frequency values are in the range  $3055\text{-}3067\text{cm}^{-1}$ , showing the following correlations:

$$\nu_{\text{sym}} (\text{CH str. } (3067 \text{ cm}^{-1})) > \nu_{\text{asym}} (\text{CH str.}) (3055\text{cm}^{-1})$$

**-For armchair molecule:**

Their frequency values are in the range  $3083\text{-}3046 \text{ cm}^{-1}$ . Indicating the following relation:

$$\nu_{\text{sym}} (= \text{CH str.}) (3083 \text{ cm}^{-1}) > \nu_{\text{asym}} (= \text{CH str.}) (3046 \text{ cm}^{-1})$$

(A<sub>1</sub>) (B<sub>1</sub>)

**-For chiral molecule:**

Their frequency values are in the range  $3032\text{-}3057 \text{ cm}^{-1}$ , showing the following correlations:

$$\nu_{\text{sym}} (\text{CH str.}) (3057 \text{ cm}^{-1}) > \nu_{\text{asym}} (\text{CH str.}) (3054 \text{ cm}^{-1})$$

(A<sub>1g</sub>) (E<sub>g</sub>)

**For the three molecules the relation**

$$\nu_{\text{sym}} (\text{CH str.}) > \nu_{\text{asym}} (\text{CH str.})$$

**holds**

**-For zig-zag molecule:**

Calculated CC stretching vibration frequencies are in the range  $1382\text{-}1565 \text{ cm}^{-1}$ . Showing the following correlation;

**Ring (CC stretching) vibrations**

$$\nu_{\text{sym.}} (\text{CC str.}) (1531 \text{ cm}^{-1}) (\text{axial.}) > \nu_{\text{asym.}} (\text{CC str.}) (1457 \text{ cm}^{-1}) (\text{axial.})$$

(A<sub>1g</sub>) (A<sub>1u</sub>)

$$\nu_{\text{sym.}} (\text{CC str.}) (1531 \text{ cm}^{-1}) (\text{axial.}) > \nu_{\text{asym.}} (\text{CC str.}) (1411 \text{ cm}^{-1}) (\text{circum.})$$

(A<sub>1g</sub>) (B<sub>1g</sub>)

$$\text{In general } \nu_{\text{sym.}} (\text{CC str.}) > \nu_{\text{asym.}} (\text{CC str.})$$

**-For armchair molecule:**

Calculated vibration frequencies are in the range  $1334\text{-}1635$

$\text{cm}^{-1}$ . They show the following relations;

$$\nu_{\text{sym}} (\text{C=C str.}) (1634 \text{ cm}^{-1}) < \nu_{\text{asym}} (\text{C=C str.}) (1635 \text{ cm}^{-1}) \quad \text{circum.}$$

(A<sub>1</sub>) (E<sub>1</sub>)

$$\begin{aligned} \nu_{\text{sym}} (\text{C--C str.}) (1406 \text{ cm}^{-1}) &< \nu_{\text{asym}} (\text{C--C str.}) (1596 \text{ cm}^{-1}) && \text{axial} \\ &(\text{A}_1) && (\text{B}_1) \\ \nu_{\text{sym}} (\text{C-C str.}) (1334 \text{ cm}^{-1}) &< \nu_{\text{asym}} (\text{C-C str.}) (1379 \text{ cm}^{-1}) && \text{circum.} \\ &(\text{A}_1) && (\text{E}_2) \end{aligned}$$

In general  $\nu_{\text{sym}} (\text{C-C str.}) < \nu_{\text{asym}} (\text{C-C str.})$

This relation is reverse to that in zig-zag molecule because the C-Ca bonds become as a C-Cc bonds in armchair molecules.

Calculated vibration frequencies are in the range 1342-1638  $\text{cm}^{-1}$ . They show the following relations;

**-For chiral molecule:**

$$\begin{aligned} \nu_{\text{sym}} (\text{C=C str.}) (1637 \text{ cm}^{-1}) &< \nu_{\text{asym}} (\text{C=C str.}) (1642 \text{ cm}^{-1}) && (\text{circum.}) \\ &(\text{A}_{1g}) && (\text{E}_g) \\ \nu_{\text{sym}} (\text{C--C str.}) (1602 \text{ cm}^{-1}) &< \nu_{\text{asym}} (\text{C--C str.}) (1642 \text{ cm}^{-1}) && (\text{axial}) \\ &(\text{A}_{1g}) && (\text{A}_{1u}) \end{aligned}$$

**And generally:**

$$\nu (\text{C-C str.}) (\text{circum.}) < \nu (\text{C--C str.}) (\text{axial.}) < \nu (\text{C=C str.}) (\text{circum.})$$

### Ring (CCC stretching vibrations)

Unlike the C-C vibration modes, these are not located at definite C atoms as could be seen from the atomic displacement vectors. Their frequencies are lower than those of the C-C vibration modes.

According to the calculating results, the range of these frequencies are 1300-1347  $\text{cm}^{-1}$  for zigzag molecule, 1359-1406  $\text{cm}^{-1}$  for armchair molecule, and 1358-1454  $\text{cm}^{-1}$  for chiral molecule.

### Bending (CCC) vibrations ( $\delta\text{CCC}$ )

Of smaller values are the deformation ( $\delta\text{CCC}$ ) vibrations. According to their assignment, they fall in the range 431-1228  $\text{cm}^{-1}$  for zigzag molecule. These modes include the expected clock and anticlockwise vibration motions.

### -For armchair molecule:

Their calculated frequencies are in the range 448-1155  $\text{cm}^{-1}$ .

### -For chiral molecule:

Their calculated frequencies are in the range 833-1102  $\text{cm}^{-1}$ .

Generally for the three molecules, the symmetric modes are of higher frequencies than the asymmetric.

### Bending CH vibrations ( $\delta\text{CH}$ )

Their displacement vectors are mainly located at the corresponding H atoms.

### -For zigzag molecule:

The calculated frequency values are in the range 1107-1288  $\text{cm}^{-1}$ .

### -For armchair molecule:

Their calculated frequencies are in the range 1180-1474  $\text{cm}^{-1}$ .

**-For chiral molecule:**

The calculated frequencies are in the range 1164-1484  $\text{cm}^{-1}$ , with the following correlation:

$$v_{\text{sym.}} \delta(--\text{CH}) (\text{rock.}) > v_{\text{sym.}} \delta(--\text{CH}) (\text{sciss.})$$

$$v_{\text{sym.}} \delta(--\text{CH}) (\text{sciss.}) > v_{\text{sym.}} \delta(=\text{CH}) (\text{sciss.})$$

$$v_{\text{asym.}} \delta(=\text{CH}) (\text{rock.}) > v_{\text{asym.}} \delta(=\text{CH}) (\text{sciss.})$$

$$v_{\text{sym}} (\gamma\text{CH}) (\text{wag.}) (956 \text{ cm}^{-1}) > v_{\text{asym}} (\gamma\text{CH}) (\text{twist.}) (860 \text{ cm}^{-1})$$

(A<sub>1g</sub>) (B<sub>1g</sub>)

$$v_{\text{asym}} (\gamma\text{CH}) (\text{wag.}) (936 \text{ cm}^{-1}) > v_{\text{asym}} (\gamma\text{CH}) (\text{twist.}) (904 \text{ cm}^{-1})$$

(E<sub>1g</sub>) (E<sub>2g</sub>)

**-For armchair molecule:**

The ( $\gamma\text{CH}$ ) out of plane vibration frequencies are in the range 706-993  $\text{cm}^{-1}$ .

**-For chiral molecule:**

The calculated frequencies are in the range 682-997  $\text{cm}^{-1}$ , with the following relations:

$$v_{\text{asym.}} \gamma(=\text{CH}) (\text{twist.}) \text{ circum.} >$$

$$v_{\text{asym.}} \gamma(--\text{CH}) (\text{twist.}) (\text{axial.})$$

$$v_{\text{sym.}} \gamma(=\text{CH}) (\text{wag.}) \text{ circum.} <$$

$$v_{\text{asym.}} \gamma(--\text{CH}) (\text{twist.}) (\text{axial.})$$

$$v_{\text{sym.}} \gamma(=\text{CH}) (\text{wag.}) \text{ circum.} <$$

$$v_{\text{sym.}} \gamma(--\text{CH}) (\text{wag.}) (\text{axial.})$$

**Ring out of plane vibrations ( $\gamma\text{CCC}$ )**

The ring out of plane vibrations ( $\gamma\text{CCC}$ ), show frequencies values of which the range is 133-768  $\text{cm}^{-1}$ . The modes include puckering, deformations, as well as breathing vibrations of the whole ring. The relation of the sym. to the asym. modes for zigzag molecule is viewed in the following scheme;

**Out of plane vibration frequencies****( $\gamma\text{CH}$ )****-For the zigzag molecule:**

The ( $\gamma\text{CH}$ ) out of plane vibration frequencies are in the range 817-956  $\text{cm}^{-1}$ . The following relations hold too;

$$v_{\text{sym.}} (\gamma\text{CCC}) (\text{axial.}) (537 \text{ cm}^{-1}) > v_{\text{sym.}} (\gamma\text{CCC}) (\text{circum.}) (462 \text{ cm}^{-1})$$

(A<sub>1g</sub>)

(A<sub>1g</sub>)

$$v_{\text{asym.}} (\gamma\text{CCC}) (\text{axial.}) (768 \text{ cm}^{-1}) >$$

$$v_{\text{asym.}} (\gamma\text{CCC}) (\text{circum.}) (658 \text{ cm}^{-1})$$

(E<sub>1g</sub>)

(E<sub>1g</sub>)

$$v_{\text{sym.}} (\gamma\text{CCC}) (\text{axial.}) (537 \text{ cm}^{-1}) >$$

$$v_{\text{asym.}} (\gamma\text{CCC}) (\text{axial.}) (324 \text{ cm}^{-1})$$

(A<sub>1g</sub>)

(B<sub>1u</sub>)

$$v_{\text{sym.}} (\gamma\text{CCC}) (\text{circum.}) (462 \text{ cm}^{-1}) >$$

$$v_{\text{asym.}} (\gamma\text{CCC}) (\text{circum.}) (331 \text{ cm}^{-1})$$

(A<sub>1g</sub>)

(B<sub>1g</sub>)

**-For armchair molecule:**

The calculated frequencies range is (187-865  $\text{cm}^{-1}$ ).



**-For chiral molecule:**

The calculated frequencies range is (64-765  $\text{cm}^{-1}$ ), with the following relations:

$$\nu_{\text{sym.}} (\gamma\text{CCC}) (616 \text{ cm}^{-1}) < \nu_{\text{asym.}} (\gamma\text{CCC}) (765 \text{ cm}^{-1})$$

$$(A_{1g}) \qquad \qquad \qquad (A_{1u})$$

Table 2 includes the calculated frequencies and IR absorption intensities of the vibration modes of the zigzag molecule as a sample of the calculation and assignment results. Commonly known, the vibrations with (intensity= 0.0) are IR forbidden, those with (intensity $\neq$  0.0) are IR allowed.

The vibration modes in the table are classified according to the Herzberg scheme<sup>[25]</sup>.

Figure 5 shows the vibration pictures for some modes of the [6] Cyclacene (zig zag) molecule, as calculated applying the DFT method.

**Table (2): Calculated vibration frequencies and IR absorption intensities for [6] Cyclacene (zig zag) molecule.**

Symmetry & description		PM3 Freq. $\text{cm}^{-1}$	(DFT) B3LYP/ 6-311G Freq. $\text{cm}^{-1}$	Intensity km/mol
<b>A<sub>1g</sub></b>				
v <sub>1</sub>	CH str.	3073	3067	0.000
v <sub>2</sub>	ring (CC str.) (axial b.)	1644	1531	0.000
v <sub>3</sub>	$\gamma$ CH (wag.)	950	956	0.000
v <sub>4</sub>	$\delta$ ring ( $\delta$ CCC) (elongation)	890	775	0.000
v <sub>5</sub>	$\gamma$ ring ( $\gamma$ CCC) (axial b.) (breath.)	538	537	0.000
v <sub>6</sub>	$\gamma$ ring ( $\gamma$ CCC) (circum. b.) (breath.)	452	462	0.000
<b>B<sub>1g</sub></b>				
v <sub>7</sub>	CH str.	3072	3055	0.000
v <sub>8</sub>	ring (CC str.) (circum. b)	1600	1411	0.000
v <sub>9</sub>	$\gamma$ CH (twist.)	867	860	0.000
v <sub>10</sub>	$\gamma$ CH (twist.) + $\gamma$ ring ( $\gamma$ CCC)	782	817	0.000
v <sub>11</sub>	$\gamma$ ring ( $\gamma$ CCC) (circum. b.) (puck.)	330	331	0.000
<b>A<sub>1u</sub></b>				
v <sub>12</sub>	ring (CC str.) (circum. b.) + $\delta$ CH rock.)	1717	1388	0.000
v <sub>13</sub>	$\delta$ CH (rock.) + $\delta$ ring ( $\delta$ CCC) (axial. b.)	1119	1107	0.000
v <sub>14</sub>	$\delta$ ring ( $\delta$ CCC) (clock & anticlock wise)	453	431	0.000

<b>B<sub>1u</sub></b>				
v <sub>15</sub>	ring (CC str.) (axial b.) + $\delta$ CH (sciss.)	1583	1457	0.000
v <sub>16</sub>	ring (CCC str.) (axial b.)	1377	1363	0.000
v <sub>17</sub>	ring ( $\delta$ CCC) + $\delta$ CH (sciss.)	979	903	0.000
v <sub>18</sub>	$\gamma$ ring ( $\gamma$ CCC) (axial b.) (puck.)	358	324	0.000
<b>E<sub>1g</sub></b>				
v <sub>19</sub>	CH str.	3071	3061	0.000
v <sub>20</sub>	CH str.	3071	3061	0.000
v <sub>21</sub>	ring (CC str.) (cercum. b)	1694	1565	0.000
v <sub>22</sub>	ring (CC str.) (cercum. b)	1694	1565	0.000
v <sub>23</sub>	$\delta$ CH + $\delta$ ring ( $\delta$ CCC)	1384	1288	0.000
v <sub>24</sub>	$\delta$ CH + $\delta$ ring ( $\delta$ CCC)	1384	1288	0.000
v <sub>25</sub>	$\delta$ CH + $\delta$ ring ( $\delta$ CCC)	1145	1207	0.000
v <sub>26</sub>	$\delta$ CH + $\delta$ ring ( $\delta$ CCC)	1145	1207	0.000
v <sub>27</sub>	$\gamma$ CH (wag.)	925	936	0.000
v <sub>28</sub>	$\gamma$ CH (wag.)	925	936	0.000
v <sub>29</sub>	$\gamma$ ring ( $\gamma$ CCC) (axial. b.) (puck.)	827	768	0.000
v <sub>30</sub>	$\gamma$ ring ( $\gamma$ CCC) (axial. b.) (puck.)	827	768	0.000
v <sub>31</sub>	$\gamma$ ring ( $\gamma$ CCC) (cercum. b.) (puck.)	638	658	0.000
v <sub>32</sub>	$\gamma$ ring ( $\gamma$ CCC) (cercum. b.) (puck.)	638	658	0.000
v <sub>33</sub>	$\gamma$ ring ( $\gamma$ CCC) (puck.)	329	333	0.000
v <sub>34</sub>	$\gamma$ ring ( $\gamma$ CCC) (puck.)	329	333	0.000
<b>E<sub>1u</sub></b>				
v <sub>35</sub>	CH str.	3073	3062	20.066
v <sub>36</sub>	CH str.	3073	3062	20.066
v <sub>37</sub>	ring (CC str.) (axial b.) + $\delta$ CH (rock.)	1632	1516	3.559
v <sub>38</sub>	ring (CC str.) (axial b.) + $\delta$ CH (rock.)	1632	1516	3.559
v <sub>39</sub>	ring (CCC str.) (axial b.)	1479	1347	32.422
v <sub>40</sub>	ring (CCC str.) (axial b.)	1479	1347	32.422
v <sub>41</sub>	$\delta$ CH (rock.) + ring (CCC str.)	1156	1201	0.117
v <sub>42</sub>	$\delta$ CH (rock.) + ring (CCC str.)	1156	1201	0.117
v <sub>43</sub>	$\gamma$ CH (twist.)	927	910	557.652
v <sub>44</sub>	$\gamma$ CH (twist.)	927	910	557.652
v <sub>45</sub>	$\delta$ ring ( $\delta$ CCC) (axial b.) (elongation)	894	762	5.054
v <sub>46</sub>	$\delta$ ring ( $\delta$ CCC) (axial b.) (elongation)	894	762	5.054

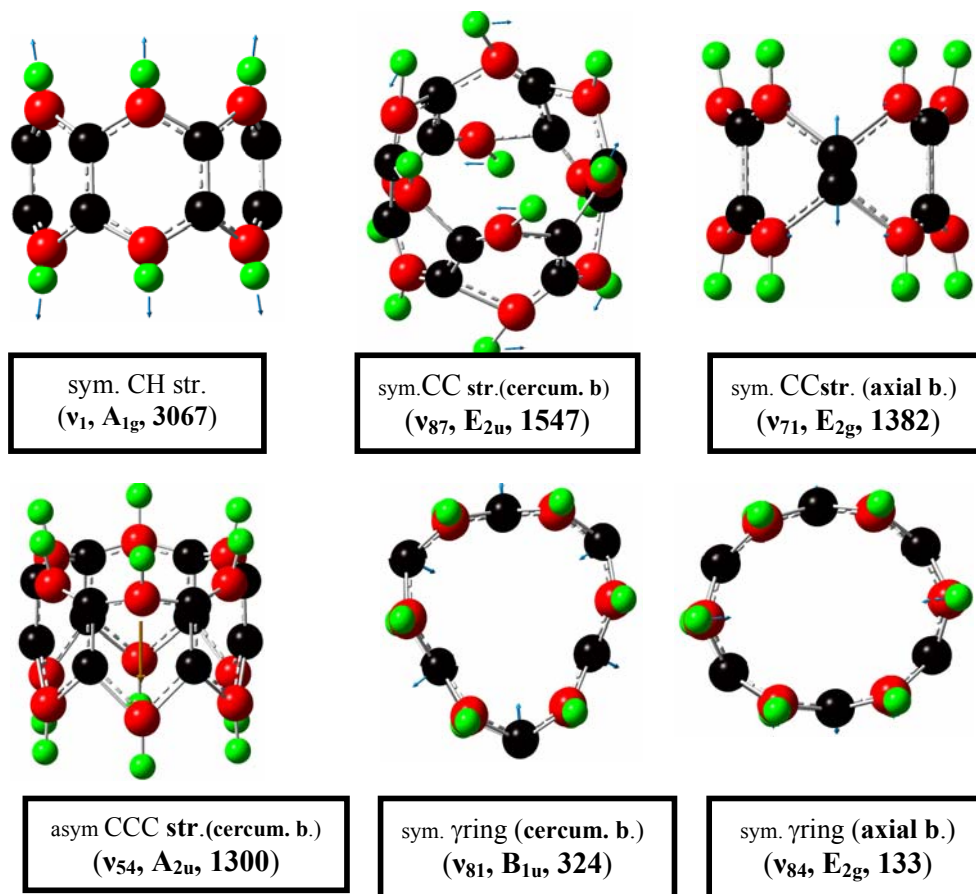
v <sub>47</sub>	$\delta$ ring ( $\delta$ CCC) ( <b>cercum. b.</b> )	594	585	19.554
v <sub>48</sub>	$\delta$ ring ( $\delta$ CCC) ( <b>cercum. b.</b> )	594	585	19.554
v <sub>49</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>cercum. b.</b> ) ( <b>puck.</b> )	443	403	8.433
v <sub>50</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>cercum. b.</b> ) ( <b>puck.</b> )	443	403	8.433
<b>A<sub>2g</sub></b>				
v <sub>51</sub>	ring (CC <b>str.</b> ) ( <b>circum. b., clock &amp; anti clockwise</b> ) + $\delta$ CH	1248	1504	0.000
v <sub>52</sub>	$\delta$ CH ( <b>rock.</b> ) ( <b>clock &amp; anticlockwise</b> )	1090	1227	0.000
<b>A<sub>2u</sub></b>				
v <sub>53</sub>	<b>CH str.</b>	3072	3064	58.588
v <sub>54</sub>	ring (CCC <b>str.</b> ) ( <b>cercum. b.</b> ) + $\delta$ CH	1404	1300	90.410
v <sub>55</sub>	$\gamma$ CH ( <b>wag.</b> )	928	922	378.955
v <sub>56</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial. b.</b> ) ( <b>puck.</b> )	809	735	131.157
v <sub>57</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>cercum. b.</b> ) ( <b>puck.</b> )	418	382	76.438
<b>B<sub>2g</sub></b>				
v <sub>58</sub>	ring (CC <b>str.</b> ) ( <b>cercum. b.</b> )	1556	1432	0.000
v <sub>59</sub>	$\delta$ CH ( <b>sciss.</b> ) + ring ( $\delta$ CCC)	1207	1274	0.000
v <sub>60</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial. b.</b> ) ( <b>puck.</b> )	678	665	0.000
v <sub>61</sub>	ring ( $\delta$ CCC) ( <b>cercum. b.</b> )	475	466	0.000
<b>B<sub>2u</sub></b>				
v <sub>62</sub>	<b>CH str.</b>	3073	3056	0.000
v <sub>63</sub>	ring (CCC <b>str.</b> ) + $\delta$ CH ( <b>sciss.</b> )	1573	1320	0.000
v <sub>64</sub>	$\gamma$ CH ( <b>twist.</b> )	832	876	0.000
v <sub>65</sub>	ring ( $\delta$ CCC) + $\delta$ CH ( <b>sciss.</b> )	598	599	0.000
v <sub>66</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial. b.</b> ) ( <b>puck.</b> )	281	255	0.000
<b>E<sub>2g</sub></b>				
v <sub>67</sub>	<b>CH str.</b>	3073	3058	0.000
v <sub>68</sub>	<b>CH str.</b>	3073	3058	0.000
v <sub>69</sub>	ring (CC <b>str.</b> )( <b>axial. b.</b> ) + $\delta$ CH ( <b>sciss.</b> )	1608	1497	0.000
v <sub>70</sub>	ring (CC <b>str.</b> )( <b>axial. b.</b> ) + $\delta$ CH ( <b>sciss.</b> )	1608	1497	0.000
v <sub>71</sub>	ring (CC <b>str.</b> ) ( <b>axial. b. + cercum. b.</b> )	1576	1382	0.000
v <sub>72</sub>	ring (CC <b>str.</b> ) ( <b>axial. b. + cercum. b.</b> )	1576	1382	0.000
v <sub>73</sub>	$\delta$ CH + ( $\delta$ CCC)	1280	1271	0.000
v <sub>74</sub>	$\delta$ CH + ( $\delta$ CCC)	1280	1271	0.000
v <sub>75</sub>	$\gamma$ CH ( <b>twist.</b> )	961	904	0.000
v <sub>76</sub>	$\gamma$ CH ( <b>twist.</b> )	961	904	0.000

v <sub>77</sub>	$\gamma$ CH ( <b>twist.</b> ) + $\gamma$ ring ( $\gamma$ CCC)	864	845	0.000
v <sub>78</sub>	$\gamma$ CH ( <b>twist.</b> ) + $\gamma$ ring ( $\gamma$ CCC)	864	845	0.000
v <sub>79</sub>	$\delta$ ring ( $\delta$ CCC) ( <b>circum b.</b> ) ( <b>elongation</b> )	627	619	0.000
v <sub>80</sub>	$\delta$ ring ( $\delta$ CCC) ( <b>circum b.</b> ) ( <b>elongation</b> )	627	619	0.000
v <sub>81</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>circum. b.</b> ) ( <b>puck.</b> )	405	387	0.000
v <sub>82</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>circum. b.</b> ) ( <b>puck.</b> )	405	387	0.000
v <sub>83</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial b.</b> ) ( <b>puck.</b> )	147	133	0.000
v <sub>84</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial b.</b> ) ( <b>puck.</b> )	147	133	0.000
<b>E<sub>2u</sub></b>				
v <sub>85</sub>	CH <b>str.</b>	3072	3056	0.000
v <sub>86</sub>	CH <b>str.</b>	3072	3056	0.000
v <sub>87</sub>	ring (CC <b>str.</b> ) ( <b>circum. b</b> )	1685	1547	0.000
v <sub>88</sub>	ring (CC <b>str.</b> ) ( <b>circum. b</b> )	1685	1547	0.000
v <sub>89</sub>	ring (CCC <b>str.</b> ) + $\delta$ CH ( <b>sciss.</b> )	1428	1308	0.000
v <sub>90</sub>	ring (CCC <b>str.</b> ) + $\delta$ CH ( <b>sciss.</b> )	1428	1308	0.000
v <sub>91</sub>	$\delta$ ring ( $\delta$ CCC) ( <b>circum. b</b> )	1196	1228	0.000
v <sub>92</sub>	$\delta$ ring ( $\delta$ CCC) ( <b>circum. b</b> )	1196	1228	0.000
v <sub>93</sub>	$\gamma$ CH ( <b>twist.</b> )	885	892	0.000
v <sub>94</sub>	$\gamma$ CH ( <b>twist.</b> )	885	892	0.000
v <sub>95</sub>	$\gamma$ CH ( <b>twist.</b> ) + $\gamma$ ring ( $\gamma$ CCC)	846	839	0.000
v <sub>96</sub>	$\gamma$ CH ( <b>twist.</b> ) + $\gamma$ ring ( $\gamma$ CCC)	846	839	0.000
v <sub>97</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial. b.</b> ) ( <b>puck.</b> )	672	670	0.000
v <sub>98</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>axial. b.</b> ) ( <b>puck.</b> )	672	670	0.000
v <sub>99</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>circum. b</b> ) ( <b>puck.</b> )	430	429	0.000
v <sub>100</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>circum. b</b> ) ( <b>puck.</b> )	430	429	0.000
v <sub>101</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>circum. b</b> ) ( <b>puck.</b> )	181	185	0.000
v <sub>102</sub>	$\gamma$ ring ( $\gamma$ CCC) ( <b>circum. b</b> ) ( <b>puck.</b> )	181	185	0.000

$\gamma$ : Out of plane of the molecule.,  $\delta$ : In- plane of the molecule.

(**breath.**): ring breathing mode., (**puck.**): ring puckering mode. , (**sciss.**): CH scissoring mode.

(**twist.**): CH twisting mode., (**wag.**): CH wagging mode.

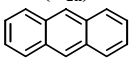
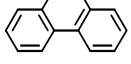
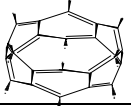
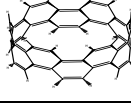
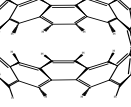


**Figure 5. The graphical pictures of some vibration modes for [6] Cyclacene (zigzag) molecule as calculated applying the DFT method.**

Table 3 shows comparison of the calculated vibration frequencies of [6] cyclacenes molecules with the frequencies of anthracene and phenanthrene molecules by using the same level of DFT theory, the frequency values of [6] cyclacenes are

lower. The comparison shows that the force field for cyclacene is weaker than that of the coplanar polyaromatic molecule. It indicates the influence of folding in diminishing the C-C bond strength of the aromatic molecule too.

**Table 3: Comparison of the calculated vibration frequencies of [6] cyclacene molecules with those of coplanar anthracene and phenanthrene molecules using B3LYP/6-311G .**

Molecule	C-H sym.	C-H asym.	C-Ca sym.	C-Ca asym.	C-Cc sym.	C-Cc asym.	$\delta$ CH sym.	$\delta$ CH asym.	$\gamma$ CH sym.	$\gamma$ CH asym.
Anthracene ( $D_{2h}$ ) 	3156 $A_g$	3153 $B_{1u}$	1592 $A_g$	1582 $B_{2u}$	-----	1670 $B_{1u}$	1302A g-	1320 $B_{3g}$	-----	992 $B_{1g}$
Phenanthrene ( $C_{2v}$ ) 	3209 $A_1$	3198 $B_2$	1644 $A_1$	1656 $B_1$	1662 $A_1$	-----	1341 $A_1$	1328 $B_2$	1005 $A_2$	1021 $B_1$
[6] Cyclacene zig-zag ( $D_{6h}$ ) 	3067 $A_{1g}$	3055 $B_{1g}$	1531 $A_{1g}$	1457 $B_{1u}$	-----	1411 $B_{1g}$	1222 $A_{1g}$	1274 $B_{2g}$	-----	992 $B_{1g}$
[6] Cyclacene armchair ( $D_{6d}$ ) 	3083 $A_1$	3046B 1	1406 $A_1$	1496 $B_1$	1634 $A_1$	1635 $E_1$	1222 $A_1$	1214 $E_1$	810 $A_1$	963 $B_1$
[6] Cyclacene chiral ( $D_{3d}$ ) 	3057 $A_{1g}$	3042 $A_{1u}$	1602 $A_{1g}$	1642 $A_{1u}$	1637 $A_{1g}$	1641 $E_g$	1224 $A_{1g}$	1244 $A_{1u}$	933 $A_{1g}$	915 $E_g$

The result parallels that of Turker<sup>[26]</sup> who showed, on the basis of the Hückel treatment, that the electronic binding energy of the planar polyaromatic hydrocarbon are bigger in value than those of the cyclacene molecule with similar number of benzene rings.

## References

- 1-M. Kaempgen, G. S. Duesberg and S. Roth, *Appl. Surf. Sci.*, 2005, **252(2)**, 425-429.
- 2- I. Lukovitz, F. H. Karman, P. M. Nagy and E. Kalman, *Croat. Chim. Acta*, 2007, **80**, 233-237.
- 3- T. Yao, Hao Yu, R. J. Vermelj and G. J. Bodwell, *Phys., J. Am. Rev. Lett.* **80**, 1-3.
- 4- M. S. Dresselhaus, G. Dresselhaus and P. Avouris, *Carbon Nanotubes, Synthesis, Structures, Properties and Applications*, Springer- Verlag, New York, 1996.
- 5- N. Anderson, A. Hartschuh, S. Cronin and L. Novotny, *J. Am. Chem. Soc.* 2005, **127**, 2533-2537.
- 6- S. Iijima, *Nature*, 1991, **354**, 56-58 ; S. Iijima, T. Ichihashi, *Nature*, 1993, **363**, 603-605.
- 7- N. Hamada, S. Sawada, A. Oshiyama, *Phys. Rev. Lett.*, 1992, **68**, 1579-1581.

- 8- Y. Wang and X. Jing, *Polym. Adv. Technol.*, 2005, **16**, 344.
- 9- T. Durkop, S.A. Getty, E. Cobas and M.S. Fuhrer, *Nano Lett.*, 2004, **4**, 35-39.
- 10- B.I. Yacobson and R.E. Smalley, *American Scientist*, 1997, **85**, 324-337.
- 11- R. Gleiter, B. Esser and S. Kornmeyer, *Acc. Chem. Res.*, 1983, **16**, 328-334.
- 12- M. Shanshal, *Turk. J. Chem.*, 2010, **34**, 269-275.
- 13- W. Kohn, and L. J. Sham, *Phys. Rev.*, 1965, **140**, A1133-A1138, P. Hohenberg, and W. Kohn, *Phys. Rev.*, 1964, **136**, B864-B871.
- 14- R. G. Parr and W. Yang, "Density-Functional Theory of Atoms and Molecules," Oxford, New York, p. 53, 1989; E. Wilson, Chem. Eng. News, 1998, October 19, 12; D. Malakoff, Science, **282**, 610, 1998.
- 15- 6- 311G, See G03, Manual, Gaussian, Inc. Pittsburgh, PA, 2003.
- 16- J. J. P. Stewart, *J. Comp. Chem.*, 1989, **10**, 209; J. J. P. Stewart, *J. Comp. Chem.*, 1989, **10**, 221; J. J. P. Stewart, *J. Comp. Chem.*, 1991, **12**, 320; M. J. S. Dewar, E. F. Healy, A. J. Holder, and Y. C. Yuan, *J. Comp. Chem.*, 1990, **11**, 541.
- 17- M.J. Frish, Gaussian 03, Revision B.03, Gaussian Pittsburgh, PA., 2003.
- 18- L. Vitali, M. Burghard, M.A. Schneider, Y. Wu, Lei Liu, C. Jayanthi and K. Kern, *Phys. Rev. Lett.*, 2004, **93**, 136103.
- 19- R. Saito, G. Dresselhaus, M. S. Dresselhaus, *Phys. Rev*, 2000, **B 61**, 2981.
- 20- a- U. Kuhlman, H. Jantoljak, N. Pfander, P. Bernier, C. Journet and C. Thomsen, *Chem. Phys. Lett.*, 198, **294**, 237-240, b- U. Kuhlman, H. Jantoljak, N. Pfander, C. Journet, P. Bernier, and C. Thomsen, *Synth. Met.*, 1999, **103**, 2506-2507.
- 21- K.A. Ramani and H. Chadl, *J. Phys. chem.*, 2006, **B 110 (25)**, 12388-12393.
- 22- A.B. Dalton, J.N. Coleman, B. McCarthy, P.M. Ajayan, S. Lefrant, P. Bernier, W. Blau and H.J. Byrne, *J. Phys. Chem.*, 2000, **B 104**, 10012.
- 23- a- A. Rochefort, P. Avouris, *J. Phys. Chem.*, 2000, **A 104**, 9807-9811; b- L. Chico, L.X. Benedict, S.G. Louie, M.L. Cohen, *Phys. Rev.*, 1996, **B 54**, 2600-2606; c- P.E. Pehrsson, W. Zhao, J.W. Baldwin, C.H. Song, J. Liu, S. Kooi, B. Zheng, *J. Phys. Chem.*, 2003, **B 107**, 5690-5695.
- 24- G. Davidson, "Introduction to group theory for Chemists", Applied Science Publishers Ltd. London, Elsevier Publishing Comp. Ltd., 1990.
- 25- G. Herzberg, "Molecular Spectra and Molecular Structure, Infrared and Raman Spectra of Polyatomic Molecules", van Nostrand Co. New York, 1971.
- 26- L. Turker, *Turk. J. Chem.*, 2000, **24**, 217-222.